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=====
c    bisect: Uses bisection to find approximate root
c    of f(x) on interval [xmin .. xmax]. Return value is
c    root located to (relative) tolerance 'xtol'. Return code
c    'rc' is set to 0 on success, non-zero on failure
c    and routine succeeds (by definition) as long as initial
c    interval *does* bracket at least one root. Routine
c    performs tracing of algorithm (on stderr) if input
c    argument 'trace' is .true.
=====

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```

real*8 function bisect(f,xmin,xmax,xtol,trace,rc)

```

```

    implicit      none

```

```

    real*8        drelabs

```

```

    real*8        f

```

```

    external      f

```

```

    real*8        xmin,          xmax,          xtol

```

```

    logical       trace

```

```

    integer       rc

```

```

-----
c    Other variables needed for search.

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```

    integer       mxiter

```

```

    parameter    ( mxiter = 50 )

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```

    real*8        xlo,          dx,          sgn

```

```

    integer       iter

```

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c-----
c      Check that input interval is specified correctly
c      and that it manifestly brackets at least one root:
c      (i.e. the fcn changes sign).
c-----
      if( xmax .le. xmin .or.
&        f(xmin) * f(xmax) .gt. 0.0d0 ) then
          write(0,*) 'bisect: Input interval is not '//
&                  'bracketing'
          rc = 1
c-----
c      Returned value is meaningless in this case,
c      but have to return *some* value.
c-----
          bisect = xmin
          return
      end if
c-----
c      Compute 'sgn' such that sgn * f(xmin) < 0, and
c      initialize bracketing interval
c-----
          sgn = 1.0d0
          if( f(xmin) .le. 0.0d0 ) then
              sgn = 1.0d0
          else
              sgn = -1.0d0
          end if
          xlo = xmin
          dx  = xmax - xmin

```

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c-----
c      Bisection loop: continue until root found to
c      specfied tolerance or until maximum number of
c      iterations taken
c-----
      do iter = 1 , mxiter
        bisect = xlo + 0.5d0 * dx
        if( trace ) then
          write(0,*) xlo, xlo + dx, f(bisect)
        end if
        if( sgn * f(bisect) .lt. 0.0d0 ) then
          xlo = bisect
        end if
        if( drelabs(dx,bisect,1.0d-10) .le. xtol ) go to 900
        dx = 0.5d0 * dx
      end do

900    continue
      rc = 0
      if( trace ) write(0,*)
      return

end

```

```

=====
c      drelabs:  Function useful for 'relativizing' quantity
c      being monitored for detection of convergence.
=====
      real*8 function drelabs(dx,x,xfloor)
          implicit      none

          real*8          dx,      x,      xfloor

          if( abs(x) .lt. abs(xfloor) ) then
              drelabs = abs(dx)
          else
              drelabs = abs(dx/x)
          end if

          return
      end

```

```

=====
c      tbisect: Illustrates root finding using bisection
c      routine 'bisect'.
c
c      Initial bracketing interval must be specified via the
c      command-line, along with optional convergence criteria
c      and output option.
c
c      This program also illustrates the general Fortran
c      techniques (briefly discussed previously) for:
c
c      (1) Writing and using routines which take other routines
c      as arguments.
c      (2) Using a COMMON block to communicate information to
c      a routine in cases where the information cannot be
c      passed via the argument list.
c      (3) Using an "INCLUDE" file (in this case 'comf.inc')
c      to ensure that the same common block structure is defined
c      in all program units.
c
c      Currently set up for computing square roots i.e.
c      solves
c
c          f(x; a) = x**2 - a = 0
c
c      for 'a' specified on command-line
c
c      Outputs a, approximate root (x*) and f(x*; a) on stdout.
=====
      program          tbisect
      implicit        none

```

```

c-----
c   Declaration of the bisection routine.
c-----
c   real*8           bisect
c-----
c   Name of the specific function whose root we seek.
c   Note use of 'external' to let compiler know 'fsqr'
c   is the name of a function, not a variable.
c-----
c   real*8           fsqr
c   external         fsqr
c
c   integer          i4arg,           iargc
c   real*8           r8arg
c-----
c   For use in detecting bad real*8 command-line value.
c-----
c   real*8           r8_never
c   parameter        ( r8_never = -1.0d-60 )
c-----
c   Use a common block to pass number whose square root
c   is sought to external function 'fsqr'.
c-----
c   include          'comf.inc'
c-----
c   Initial bracket, convergence tolerance and output
c   option from command-line; default value for conv.
c   tolerance.
c-----
c   real*8           xmin,           xmax,           xtol
c   logical          trace
c
c   real*8           default_xtol
c   parameter        ( default_xtol = 1.0d-8 )

```

```

c-----
c   Root and return code from bisection routine.
c-----
      real*8          root
      integer         rc
c-----
c   Argument parsing.
c-----
      if( iargc() .lt. 3 ) go to 900
      a      = r8arg(1,r8_never)
      xmin  = r8arg(2,r8_never)
      xmax  = r8arg(3,r8_never)
      if( a .eq. r8_never .or. xmin .eq. r8_never .or.
&      xmax .eq. r8_never ) go to 900

      xtol  = r8arg(4,default_xtol)
      trace = iargc() .gt. 4
c-----
c   Invoke root finder then write a, sqrt(a), and residual
c   to standard output.
c-----
      root = bisect(fsqr,xmin,xmax,xtol,trace,rc)
      if( rc .eq. 0 ) then
          write(*,*) a, root, fsqr(root)
      else
          write(0,*) 'tbisect: Bisection failed.'
      end if
c-----
c   Normal exit.
c-----
      stop

```

```

c-----
c   Usage exit.
c-----
900  continue
      write(0,*) 'usage: tbisect <a> <xmin> <xmax> '//
&      '[<xtol> <trace>]'
      stop

      end

```

```

c=====
c   Function whose root is sought.  Again, note use of
c   COMMON block to pass additional information (in this
c   case 'a') to the routine.
c=====
      real*8 function fsqr(x)
          implicit      none

          real*8        x

          include       'comf.inc'

          fsqr = x**2 - a

          return
      end

```



```
c-----  
c   Common block for communicating value of 'a' from main  
c   to 'fsqr'.  
c-----  
real*8          a  
common  / comf /  a
```

```

#####
# Building 'tbisect' and sample output on sgi1
#
# 'tbisect' is set up to compute sqrt(a) via bisection.
#####

sgi1% pwd ; ls
/usr/people/phys410/nonlin/ex1

Makefile    bisect.f    comf.inc    tbisect.f
sgi1% make
f77 -g -64 -c tbisect.f
f77 -g -64 -c bisect.f
f77 -g -64 -L/usr/local/lib tbisect.o bisect.o -lp410f -o tbisect

sgi1% tbisect
usage: tbisect <a> <xmin> <xmax> [<xtol> <trace>]

#####
# Compute +sqrt(2) to default tolerance (1.0d-8)
#
# Note: Exact value to 16 digits is 1.414 2135 6237 3095
#####
sgi1% tbisect 2.0 1.0 2.0
2.0000000000000000      1.414213564246893      5.2999009625409599E-09

#####
# Recompute with higher tolerance (1.0d-12)
#####
sgi1% tbisect 2.0 1.0 2.0 1.0e-12
2.0000000000000000      1.414213562372879      -6.1084470814876113E-13

```

```
#####
# Enable tracing output by supplying 5th argument. Note
# supplying a '.' as an argument parsed by 'i4arg' or 'r8arg'
# is equivalent to specifying the default value.
#####
```

```
sgi1% tbisect 2.0 1.0 2.0 . 1
```

1.0000000000000000	2.0000000000000000	0.2500000000000000
1.0000000000000000	1.5000000000000000	-0.4375000000000000
1.2500000000000000	1.5000000000000000	-0.1093750000000000
1.3750000000000000	1.5000000000000000	6.6406250000000000E-02
1.3750000000000000	1.4375000000000000	-2.2460937500000000E-02
1.4062500000000000	1.4375000000000000	2.1728515625000000E-02
1.4062500000000000	1.4218750000000000	-4.2724609375000000E-04
1.4140625000000000	1.4218750000000000	1.0635375976562500E-02
1.4140625000000000	1.4179687500000000	5.1002502441406250E-03
1.4140625000000000	1.4160156250000000	2.3355484008789063E-03
1.4140625000000000	1.4150390625000000	9.5391273498535156E-04
1.4140625000000000	1.4145507812500000	2.6327371597290039E-04
1.4140625000000000	1.4143066406250000	-8.2001090049743652E-05
1.414184570312500	1.4143066406250000	9.0632587671279907E-05
1.414184570312500	1.414245605468750	4.3148174881935120E-06
1.414184570312500	1.414215087890625	-3.8843369111418724E-05
1.414199829101563	1.414215087890625	-1.7264334019273520E-05
1.414207458496094	1.414215087890625	-6.4747728174552321E-06
1.414211273193359	1.414215087890625	-1.0799813026096672E-06
1.414213180541992	1.414215087890625	1.6174171832972206E-06
1.414213180541992	1.414214134216309	2.6871771297010127E-07
1.414213180541992	1.414213657379150	-4.0563185166320181E-07
1.414213418960571	1.414213657379150	-6.8457083557404985E-08
1.414213538169861	1.414213657379150	1.0013031115363447E-07
1.414213538169861	1.414213597774506	1.5836612909936321E-08
1.414213538169861	1.414213567972183	-2.6310235545778937E-08
1.414213553071022	1.414213567972183	-5.2368114289436107E-09
1.414213560521603	1.414213567972183	5.2999009625409599E-09

2.0000000000000000

1.414213564246893

5.2999009625409599E-09