```
Source file: tdgesv.f
                                                                          ... and solve it. Note that 'dgsev' is general
                                                                          enough to solve A x_i = b_i for multiple right-hand-
      Test program for LAPACK "driver" routine 'dgesv'
                                                                          sides b_i. Here we have only one right-hand-side.
      which computes the solution of a real system
                                                                          Also note that the procedure performs the LU
      of linear equations: A x = b
                                                                          decomposition in place, thus destroying the
                                                                          input-matrix, it also overwrites the right-hand-side(s)
                                                                          with the solution(s). Finally, observe that we
      This version uses fixed-size 2-d arrays (size fixed at
                                                                         pass the "leading dimension" (maxn) of both 'a' and
      some maximum value commensurate with needs and/or
      available memory), illustrating another commonly used
                                                                          b' to the routine. Again, this allows us to load array
      Fortran technique to implement run-time dimensioning,
                                                                          elements in the main program as we have just done,
      PARTICULARLY FOR RANK-2 ARRAYS.
                                                                          without running into troubles due to the fact that
                                                                          these elements ARE NOT, in general all contiguous in
      This time the rules are as follows: All subroutines and
                                                                         memory. This certainly includes the current 3 x 3 case.
      functions which manipulate the array must be passed:
      The array itself.
                                                                         nrhs = 1
      (2) The "true" or "physical" dimensions;
           i.e. the dimensions in MAIN (*).
                                                                         call dgesv(n, nrhs, a, maxn, ipiv, b, maxn, info)
      (3) The "run-time" or "logical" dimensions (*).
                                                                                  info .eq. 0 ) then
      (*) More precisely, due to the nature of the FORTRAN
           subscripting computation, the leading d-1 dimensions
                                                                             Solution successful, write soln to stdout.
           must be passed for a rank-d array. In particular,
                                                                             Note the use of "implied-do-loop" to write a
                                                                            sequence of elements: the enclosing parenthesis around the "loop" are required.
           for rank-2 array (matrices), THE leading physical dimension (often denoted 'LDA' in LAPACK code), and
                                                                   С
           THE leading logical dimension (often denoted 'N') must BOTH be passed.
С
                                                                          \label{eq:write(*,*) (b(i) , i = 1 , n)} $$ else if( info .lt. 0 ) then
      Passing the physical dimensions ensures that the
      linearization/subscripting calculation is identical
                                                                            Bad argument detected.
      in all program units INCUDING MAIN---so that, e.g.,
                                                                           write(0,*) 'tdgesv1: Argument ', abs(info),
      one can safely and conveniently use a(i,j) etc. in
                                                                                        ' to dgesv() is invalid'
      Passing the logical dimensions allows us to write
      routines which function for a general case (here,
                                                                           Matrix is singular.
      typically for N x N matrices).
                                                                           write(0,*) 'tdgesv1: dgesv() detected singular ',
      Passing BOTH sets of dimensions is slightly cumbersome,
                                                                                        'matrix
      but is the price we pay in this case for convenience
                                                                          end if
      and generality.
                                                                         stop
      program
                       tdgesv
                                                                          end
      implicit
                      none
      Maximum size of linear system.
                                                                    Source file: dgesv.f
      integer
                      maxn
      parameter
                                                                          SUBROUTINE DGESV( N, NRHS, A, LDA, IPIV, B, LDB, INFO )
                     (\max = 100)
                                                                         LAPACK driver routine (version 2.0) --
      Storage for arrays.
                                                                          Univ. of Tennessee, Univ. of California Berkeley, NAG Ltd.,
                                                                          Courant Institute, Argonne National Lab, and Rice University
                       a(maxn, maxn),
                                                                          March 31, 1993
                      b(maxn)
                                                                           . Scalar Arguments .
      integer
                      ipiv(maxn)
                                                                                             INFO, LDA, LDB, N, NRHS
                                                                          INTEGER
                                       nrhs.
      integer
                      i.
                                                                           . Array Arguments .
                                                                                             IPIV( * )
                                                                          INTEGER
                                                                         DOUBLE PRECISION \, A( LDA, * ), B( LDB, * )
      Set up sample 3 x 3 system ...
      a(1,1) = 1.23d0
                                                                      Purpose
      a(1,2) = 0.24d0
      a(1,3) = -0.45d0
                                                                      DGESV computes the solution to a real system of linear equations
      a(2.1) = -0.43d0
                                                                         A * X = B.
      a(2,2) = 2.45d0
                                                                      where A is an N-by-N matrix and X and B are N-by-NRHS matrices.
      a(2,3) = 0.78d0
                                                                      The LU decomposition with partial pivoting and row interchanges is
      a(3,1) = 0.51d0
                                                                      used to factor A as
      a(3,2) = -0.68d0
                                                                         A = P * L * U,
      a(3,3) = 3.23d0
                                                                      where \mbox{\bf P} is a permutation matrix, \mbox{\bf L} is unit lower triangular, and \mbox{\bf U} is
                                                                      upper triangular. The factored form of A is then used to solve the
                                                                      system of equations A * X = B.
      b(1) = 6.78d0
```

Arguments

b(2) = -3.45d0b(3) = 1.67d0

```
N
          (input) INTEGER
          The number of linear equations, i.e., the order of the
          matrix A. N >= 0.
NRHS
          (input) INTEGER
         The number of right hand sides, i.e., the number of columns of the matrix B. NRHS >= 0.
          (input/output) DOUBLE PRECISION array, dimension (LDA,N)
Α
         On entry, the N-by-N coefficient matrix A.
On exit, the factors L and U from the factorization
          A = P*L*U; the unit diagonal elements of L are not stored.
LDA
          (input) INTEGER
          The leading dimension of the array A. LDA >= \max(1,N).
         (output) INTEGER array, dimension (N) The pivot indices that define the permutation matrix P; \\
IPIV
          row \dot{\text{i}} of the matrix was interchanged with row IPIV(i).
          (input/output) DOUBLE PRECISION array, dimension (LDB,NRHS)
         On entry, the N-by-MRHS matrix of right hand side matrix B. On exit, if INFO = 0, the N-by-NRHS solution matrix X.
LDB
          (input) INTEGER
         The leading dimension of the array B. LDB \geq \max(1,N).
INFO
          (output) INTEGER
          = 0: successful exit
         < 0: if INFO = -i, the i-th argument had an illegal value
> 0: if INFO = i, U(i,i) is exactly zero. The factorization
has been completed, but the factor U is exactly
                 singular, so the solution could not be computed.
      External Subroutines ..
    EXTERNAL
                         DGETRF, DGETRS, XERBLA
      . Intrinsic Functions ...
    INTRINSIC
    .. Executable Statements ..
    Test the input parameters.
    INFO = 0
    IF( N.LT.O ) THEN
       INFO = -1
    ELSE IF( NRHS.LT.0 ) THEN
       INFO = -2
    ELSE IF( LDA.LT.MAX( 1, N ) ) THEN
       INFO = -4
    ELSE IF( LDB.LT.MAX( 1, N ) ) THEN
       INFO = -7
    END IF
    IF( INFO.NE.O ) THEN
       CALL XERBLA( 'DGESV ', -INFO )
       RETURN
    END IF
    Compute the LU factorization of A.
    CALL DGETRF( N, N, A, LDA, IPIV, INFO )
    IF( INFO.EQ.O ) THEN
       Solve the system A*X = B, overwriting B with X.
       CALL DGETRS( 'No transpose', N, NRHS, A, LDA, IPIV, B, LDB,
    END IF
    RETURN
    End of DGESV
    END
```

Source file: lnx-output

```
# Building 'tdgesv' and sample output on lnx1
lnx1 1> pwd; ls
/home/phys410/linsys/ex1
Makefile tdgesv.f
lnx1 2> printenv LIBBLAS
-lblas
lnx1 3> cat Makefile
# IMPORTANT: Note the use of LIBBLAS which should be
# set to '-lblas' on the SGI and Linux machines.
# BLAS is a acronym for Basic Linear Algebra Subprograms
# and is a Fortran- and C-callable library which implements
# basic manipulations useful in numerical linear algebra.
.IGNORE:
F77_COMPILE = $(F77) $(F77FLAGS) $(F77CFLAGS) F77_LOAD = $(F77) $(F77FLAGS) $(F77LFLAGS)
$(F77_COMPILE) $*.f
EXECUTABLES = tdgesv
all: $(EXECUTABLES)
tdgesv: tdgesv.o
$(F77_LOAD) tdgesv.o -llapack $(LIBBLAS) -o tdgesv
clean:
rm $(EXECUTABLES)
lnx1 4> make
pgf77 -g -c tdgesv.f
pgf77 -g -L/usr/local/PGI/lib tdgesv.o -llapack -lblas -o tdgesv
lnx1 5> tdgesv
   5.426364412431639
                       -0.3257753768173936
                                            -0.4083508069894625
Source file: sun-output
\mbox{\tt\#} Building 'tdgesv' and sample output on physics, a Sun 4
# Ultra-Enterprise running SunOS 5.8
physics% pwd; ls
/home2/phys410/linsys/ex1
Makefile
         tdgesv.f
physics% make
f77 -O -c tdgesv.f
tdgesv.f:
MAIN tdgesv1:
f77 -O -L/home/choptuik/lib tdgesv.o -llapack -lblas -o tdgesv
physics% tdgesv
    5.4263644124316 -0.32577537681739 -0.40835080698946
```