

## Some Useful Maple Commands

**diff:** Compute symbolic derivatives

```
> ex1 := exp( sin(4*x) ) + ln( x^2 + sqrt(x) ) ;
```

$$ex1 := e^{\sin(4x)} + \ln(x^2 + \sqrt{x})$$

```
> diff( ex1, x ) ;
```

$$4 \cos(4x) e^{\sin(4x)} + \frac{2x + \frac{1}{2\sqrt{x}}}{x^2 + \sqrt{x}}$$

```
> diff( ex1, x$2 ) ;
```

$$-16 \sin(4x) e^{\sin(4x)} + 16 \cos(4x)^2 e^{\sin(4x)} + \frac{2 - \frac{1}{4x^{(3/2)}}}{x^2 + \sqrt{x}} - \frac{\left(2x + \frac{1}{2\sqrt{x}}\right)^2}{(x^2 + \sqrt{x})^2}$$

```
[ > diff( diff( cos(x/y) , x ) , y );
```

$$\frac{\cos\left(\frac{x}{y}\right)x}{y^3} + \frac{\sin\left(\frac{x}{y}\right)}{y^2}$$

**int: Compute symbolic integrals (anti-derivatives and definite integrals)**

```
[ > ex2 := 1 / sqrt( x^2 - a^2 );
```

$$ex2 := \frac{1}{\sqrt{x^2 - a^2}}$$

```
[ > int( ex2, x );
```

$$\ln(x + \sqrt{x^2 - a^2})$$

**A definite integral**

```
[ > int( x^2 , x = 0 .. 2 );
```

$$\frac{8}{3}$$

**Don't expect miracles!!**

$$\begin{aligned} &> \text{int}(\text{ex1}, x); \\ &\int e^{\sin(4x)} + \ln(x^2 + \sqrt{x}) dx \end{aligned}$$

**Multi-dimensional integrals are often straightforward:**

$$\begin{aligned} &> \text{ex3} := (x^3 + y^3) / (x^2 - y^2); \\ &\text{ex3} := \frac{x^3 + y^3}{x^2 - y^2} \end{aligned}$$

$$\begin{aligned} &> \text{int}(\text{int}(\text{ex3}, x), y); \\ &\frac{x^2 y}{6} - \frac{1}{3} (x - y)^3 \ln(x - y) - \frac{x y^2}{6} + \frac{11 x^3}{18} - \frac{y^3}{9} + x y^2 \ln(x - y) \\ &\quad - \ln(x - y) y x^2 \end{aligned}$$

## series and taylor: Compute power series expansions

```
[ > series(exp(x), x=0);
```

$$1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5 + O(x^6)$$

```
[ > series(exp(x), x=0, 11);
```

$$1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5 + \frac{1}{720}x^6 + \frac{1}{5040}x^7 + \frac{1}{40320}x^8 \\ + \frac{1}{362880}x^9 + \frac{1}{3628800}x^{10} + O(x^{11})$$

```
[ > taylor(exp(x), x=0);
```

$$1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5 + O(x^6)$$

```
[ > Order := 8;
```

*Order := 8*

```
[ > taylor(exp(x), x=0);
```

$$1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5 + \frac{1}{720}x^6 + \frac{1}{5040}x^7 + O(x^8)$$

```
[ > Order := 6:
```

```
[ > taylor((1 + x)^(-1), x=0, 7);  
      1 - x + x^2 - x^3 + x^4 - x^5 + x^6 + O(x^7)
```

```
[ > convert(%, 'polynom');  
      1 - x + x^2 - x^3 + x^4 - x^5 + x^6
```

```
[ > coeffs(%, 'x');  
      1, -1, 1, -1, 1, -1, 1
```

### **solve: Solve equations, including linear systems**

```
[ > eq1 := x + y + z = 6; eq2 := 2*x + y + z =  
  2; eq3 := x + y + 3*z = 3;  
      eq1 := x + y + z = 6  
      eq2 := 2x + y + z = 2  
      eq3 := x + y + 3z = 3
```

```
[ > solve( {eq1, eq2, eq3} );  
      {x = -4, z = -3/2, y = 23/2}
```

```
[ > solve( {eq1, eq2, eq3} , {x, y, z} );  
      {x = -4, z = -3/2, y = 23/2}
```

```
[ > eq[1] := c[1] + c[2] + c[3] = 6:  
[ > eq[2] := 2*c[1] + c[2] + c[3] = 2:  
[ > eq[3] := c[1] + c[2] + 3*c[3] = 3:  
[ > eq[1]; eq[2]; eq[3];
```

$$c_1 + c_2 + c_3 = 6$$

$$2c_1 + c_2 + c_3 = 2$$

$$c_1 + c_2 + 3c_3 = 3$$

```
[ > solve( {eq[1],eq[2],eq[3]},  
[ >           { c[1], c[2], c[3]} );
```

$$\left\{ c_2 = \frac{23}{2}, c_3 = \frac{-3}{2}, c_1 = -4 \right\}$$

```
[ > solve( {eq[1],eq[2],eq[3]} );
```

$$\left\{ c_2 = \frac{23}{2}, c_3 = \frac{-3}{2}, c_1 = -4 \right\}$$

# Common Mistakes and Helpful Hints

## (0) Not terminating statement with ';' or ':'

```
[ > a := int(x^2,x=0..1)
  > i
                                     a := 1/3
```

## (1) Using '=' rather than ':=' for assignment

```
[ > a = 2;
                                     1/3 = 2
  > a;
                                     1/3
```

```
[ > a := 2;
                                     a := 2
  > a;
                                     2
```

## (2) Using quotes (') rather than double quotes (") to delimit strings

```
[ > string1 := "This is a Maple string";  
      string1 := "This is a Maple string"
```

```
[ > string2 := 'This is not a Maple string';  
Error, missing operator or `;`
```

## (3) Unique syntax for programming constructs

```
[ > for i from 1 to 2 do  
  >   print(i);  
  > od;  
  
      1  
      2
```

## (4) Use 'eval' or 'op' command to display definitions

```
[ > mysum := proc(x,y) x + y end:
```

```
[ > eval(mysum);  
      proc(x, y) x + y end proc
```

```
[ > op(mysum);  
      proc(x, y) x + y end proc
```



**(5) Use 'interface(verboseproc=2)' to display system proc. defns.**

```
[ > interface(verboseproc=2) ;  
  
[ > eval(nops) ;  
      proc() option builtin; 223 end proc  
  
[ > eval(sin) ;  
proc(x::algebraic)  
local n, t, pull_out, keep_in;  
option 'Copyright (c) 1992 by the University of Waterloo. All rights reserved.' ;  
      if nargs ≠ 1 then  
          error "expecting 1 argument, got %1", nargs  
      elif type(x, 'complex(float)') then evalf('sin'(x))  
      elif type(x, '∞') then  
          if type(ℜ(x), '∞') then 'if'(type(ℑ(x), 'undefined'),  
              NumericTools:-ThrowUndefined(x), x*undefined)  
          elif type(x, 'imaginary') then x  
          else ∞ + ∞*I  
          end if  
      elif type(x, 'undefined') then  
          NumericTools:-ThrowUndefined(x, 'preserve' = 'axes')
```

**elif**

`type(x, 'SymbolicInfinity')` **and** `traperror(is(x, real)) = true`

**then** *undefined*

**elif** `type(x, 'imaginary')` **or** `type(x, '*')` **and**

`member(true, map(type, {op(x)}, 'imaginary'))` **then**

$\sinh(-I*x)*I$

**elif** `type(x, 'complex(numeric)')` **then**

**if** `csgn(x) < 0` **then**  $-\sin(-x)$  **else**  $\sin(x)$  **end if**

**elif** `type(x, '*')` **and** `type(op(1, x), 'complex(numeric)')` **and**

`csgn(op(1, x)) < 0` **then**  $-\sin(-x)$

**elif** `type(x, '*')` **and** `type(x, '&*(rational, identical(pi))')`

**then**

$t := \text{op}(1, x);$

**if**  $t < 1 / 2$  **then**  $\sin(x)$

**elif**  $t < 1$  **then**  $\sin((1 - t)*\pi)$

**elif**  $t < 2$  **then**  $-\sin((2 - t)*\pi)$

**else**  $\sin((t - 2*\text{iquo}(\text{trunc}(t), 2))*\pi)$

**end if**

**elif** `type(x, '*')` **and**

`select(type, [op(x)], 'specfunc('anything', 'csgn'))`  $\neq []$  **then**

$\text{pull\_out, keep\_in} := \text{selectremove}(\text{type}, x,$

$\text{'specfunc('anything', 'csgn')});$

$\text{pull\_out}*\sin(\text{keep\_in})$

```

elif type(x, 'specfunc'('anything', 'csgn')) then x*sin(1)
elif type(x, '+' ) and traperror(sign(x)) = -1 then -sin(-x)
elif type(x, '+' ) and has(x,  $\pi$ ) then
    t := map(proc(x)
        if type(x /  $\pi$ , 'rational') then x /  $\pi$  end if
    end proc, { op(x) });
if nops(t) = 1 then
    t := op(t);
    if t < 0 then sin(x - 2* $\pi$ *trunc(1 / 2*t) + 2* $\pi$ )
    elif t < 1 / 2 then sin(x) := 'sin'(x)
    elif t < 1 then cos(x -  $\pi$  / 2)
    elif t < 2 then -sin(x -  $\pi$ )
    else sin(x - 2* $\pi$ *trunc(1 / 2*t))
    end if
else 'sin/normal'(x)
end if
elif type(x, '*') and member( $\pi$ , [op(x)], 'n') and  $\Im(x) = 0$ 
then
    t := subsop(n = 1, x);
    n := frac(t);
    if n = 0 then 0
    elif frac(1 / 2*t - 1 / 4) = 0 then 1
    elif frac(1 / 2*t + 1 / 4) = 0 then -1

```

```
    elif frac( $t - 1 / 2$ ) = 0 then  $(-1)^{(t - 1 / 2)}$   
    else 'sin/normal'(x)  
    end if
```

```
elif type(x, 'function') and nops(x) = 1 then
```

```
    n := op(0, x);
```

```
    t := op(1, x);
```

```
    if n = 'arcsin' then t
```

```
        elif n = 'arccos' then sqrt( $1 - t^2$ )
```

```
        elif n = 'arctan' then  $t / \text{sqrt}(1 + t^2)$ 
```

```
        elif n = 'arccsc' then  $1 / t$ 
```

```
        elif n = 'arcsec' then sqrt( $1 - 1 / t^2$ )
```

```
        elif n = 'arccot' then  $1 / \text{sqrt}(1 + t^2)$ 
```

```
    else 'sin/normal'(x)
```

```
    end if
```

```
elif type(x, 'specfunc'('anything', 'JacobiAM')) then
```

```
    JacobiSN(op(x))
```

```
elif type(x, 'arctan(algebraic, algebraic)') then
```

```
    op(1, x) / sqrt(op(1, x)^2 + op(2, x)^2)
```

```
else 'sin/normal'(x)
```

```
end if
```

```
end proc
```

```
[ >
```